

SUBCLASSES OF STARLIKE AND CONVEX FUNCTIONS ASSOCIATED WITH BESSEL FUNCTIONS

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ABSTRACT. The purpose of the present paper is to determine necessary and sufficient conditions for the generalized Bessel functions of first kind to belong to two new subclasses of analytic functions.

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