

NONUNIFORM POLYNOMIAL ASYMPTOTIC BEHAVIORS FOR EVOLUTION OPERATORS IN BANACH SPACES

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ABSTRACT. The paper gives some integral characterizations of Rolewicz-type for polynomial asymptotical behaviors (stability, instability, dichotomy) of evolution operators in Banach spaces.

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