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CERTAIN SUBORDINATION RESULTS INVOLVING A CLASS OF OPERATORS

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Abstract. This paper, by applying some known results in the theory of differential subordination, obtains certain new subordination properties involving a class of operators denoted by $\Im_{\lambda,\mu}^{m}(a,c,A)$ in the open unit disk. The class of operators used is a composition structure of simple forms of differential and integral operators with the Erdélyi-Kober integral operator. Several results for this operator and also involving simpler operators $\Im_{\lambda,\mu}^{m}$ and $\widetilde{I}_{A}^{a,c}$ are mentioned and relevances with some known results are also indicated.

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