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THE PROJECTIVE UNITARY IS ALGEBRAICALLY DETERMINED POLISH GROUP

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Abstract. The purpose of this paper is to prove that, if $\mathcal{H}$ is a separable complex Hilbert space, the projective unitary group is algebraically determined Polish group.

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