

## FEKETE-SZEGÖ PROBLEM FOR SOME SUBCLASSES OF HOLOMORPHIC FUNCTIONS DEFINED BY THE COMBINATION OF OPOOLA AND BABALOLA DIFFERENTIAL OPERATORS

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ABSTRACT. Inspired by the recent works of Çağlar and Orhan [5] and Kanas and Darwish [12], we obtain the coefficient estimates and Fekete-Szegő inequalities for some new subclasses of holomorphic functions defined by the combination of Opoola and Babalola differential operators.

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2010 *Mathematics Subject Classification*. 30C55, 30C45.

*Key words and phrases*. Babalola convolution operator, Opoola differential operator, Fekete-Szegő inequalities, Holomorphic function, Starlike and convex functions of complex order.

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*Received 7 January 2022*

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