

GLOBAL IN TIME CLASSICAL SOLUTIONS FOR A CLASS OF INITIAL BOUNDARY VALUE PROBLEMS FOR THE KAWAHARA EQUATION

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ABSTRACT. In this paper, we investigate a class of initial boundary value problems for a class of the Kawahara equation. We prove existence of at least one solution and existence of at least one nonnegative solution. The arguments are based upon of recent theoretical results.

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