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ON SOME GROWTH ANALYSIS OF ENTIRE AND MEROMORPHIC FUNCTIONS IN THE LIGHT OF THEIR RELATIVE $(p, q, t)L$-TH ORDER WITH RESPECT TO ANOTHER ENTIRE FUNCTION

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Abstract. In this paper we introduce the concept of relative $(p, q, t)L$-th order and relative $(p, q, t)L$-th lower order of entire and meromorphic functions with respect to another entire function and then study some growth properties of entire and meromorphic functions on the basis of their relative $(p, q, t)L$-th order and relative $(p, q, t)L$-th lower order.

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