

LIPSCHITZ ϕ -SUMMING OPERATORS

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ABSTRACT. Let $\phi: [0, \infty[\rightarrow [0, \infty[$ be a modulus function. We introduce the notion of Lipschitz ϕ -summing operator between pointed metric spaces and give a nonlinear version of a Pietsch domination theorem for such operators.

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