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ALMOST CONTRA δ-SEMICONTINUITY IN TOPOLOGICAL SPACES

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Abstract. In this paper, we introduce and investigate the notion of almost contra δ-semicontinuous functions by utilizing δ-semiclosed sets. We obtain fundamental properties of almost contra δ-semicontinuous functions and discuss the relationships between almost contra δ-semicontinuity and other related functions.

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