HYPERBOLIC NUMBERS AND THEIR FUNCTIONS

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Abstract. In this paper we describe the algebra of hyperbolic numbers, whose introduction is inspired by an interest in the factorization of the wave operator. We study in detail their elementary functions (polynomials, trigonometric and exponential functions) as well as their inverse functions (roots, logarithms, inverse trigonometric functions).

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